

Zad. 9

$f(x, y) = e^x \sin y$, $f(0,0) = 0$
pochodna po x nie zmienia, parzyste potęgi
po y zmieniają tylko znak.

$$f(x, y) = f(0,0) + \frac{\partial f}{\partial x}(0,0)x + \frac{\partial f}{\partial y}(0,0)y + \frac{1}{2} \frac{\partial^2 f}{\partial x^2}(0,0)x^2 +$$

$$+ \frac{\partial^2 f}{\partial x \partial y}(0,0)xy + \frac{1}{2} \frac{\partial^2 f}{\partial y^2}(0,0)y^2 + \frac{1}{6} \frac{\partial^3 f}{\partial x^3}(0,0)x^3 +$$

$$+ \frac{1}{2} \frac{\partial^3 f}{\partial x^2 \partial y}(0,0)x^2y + \frac{1}{2} \frac{\partial^3 f}{\partial x \partial y^2}(0,0)xy^2 + \frac{1}{6} \frac{\partial^3 f}{\partial y^3}(0,0)y^3 + R_r(x, y)$$

$$y + xy + \frac{1}{2}x^2y - \frac{1}{6}y^3 + R_r(x, y)$$